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A Study of Water Tree Frequency Dependence and Growth Rate in Polymer

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This paper presents theoretical and experimental studies **on** the water tree (W.T.) growth rate frequency dependence. The high growth rate experienced is explained **on** the light of the simulating circuit components and parameters. The results are very sensitive to the assumed water content in tree and the original tree length. Attempts were made to correlate between W.T. theories and experimental results. The mechanisms of W.T. initiation and growth are explained.

INTRODUCTION

The extent of treeing problem is not yet defined [1]. Many investigations were carried out on the treeing phenomena **[2,3,4,5].** Water trees are initiated and grown in polymers when some insulated conductors are immersed into water **[3].** However, due to the difficulty in simulating, experimentally, water treeing phenomena, the fundamental processes of the inception and extension of treeing have not yet been understood **[6].**

WATER TREE THEORY

It has been demonstrated [7] that W.T. growth rate can be written in the form

$$
GR = \frac{1}{\delta t} \int_{r_0}^{r} \frac{dr}{E^2}
$$
 (1)

Where *GR:* rate of growth

- *r,* : initial radius of tree
- *r*: increase in length of tree
- E : applied electric field

The expression was obtained on the assumption that the resistivity of tree is very small, and the tree can withstand considerable electric field. The equivalent circuit is as shown in Figure 1, Eq. (1) can be rewritten as $GR = \frac{1}{V_0^2 \delta t} \int_{r_0}^r \left(\frac{V_0^2}{V_t^2}\right) K dr$ field. The equivalent circuit is as shown in Figure 1, Eq. (1) can be rewritten as

$$
GR = \frac{1}{V_0^2 \delta t} \int_{r_0}^r \left(\frac{V_0^2}{V_1^2}\right) K \, dr
$$

$$
= \frac{1}{V_0^2 \delta t} \int_{r_0}^r F_w K \, dr \tag{2}
$$

FIGURE 1 Water treeing equivalent circuit.

The ratio

$$
\frac{V_0}{V_t} = \frac{Y_p}{Y}
$$
 (3)

Comparing (2) and **(3),** then

$$
F_w = \frac{[(G_p + G_T)^2 + w^2 (C_p + C_T)^2]}{(G_T^2 + w^2 C_T^2)}
$$
(4)

$$
K = \frac{(r+r_0)^2 \left[\tanh^{-1} \frac{1}{\left[1 + (r+r_0)/d \right]^{\frac{1}{2}} } \right]^2}{1 + (r+r_0)/d}
$$
(5)

Considering the appropriate conductivity and permittivity

$$
F_w = \frac{(g_T + g_p r/r_0)^2 + w^2 \varepsilon_0^2 (\varepsilon_T + \varepsilon_p r/r_0)^2}{g_T^2 + w^2 C_0^2 C_T^2}
$$
(6)

When w tends to infinity,

$$
F_w = \left(1 + \frac{\varepsilon_p}{\varepsilon_R} \frac{r}{r_0}\right)^2 \tag{7}
$$

and the frequency factor is permittivity dependent; but at zero frequency the frequency factor depends on the conductivity ratio as

$$
F_w = \left(1 + \frac{g_p}{g_T} \frac{r}{r_0}\right)^2 \tag{8}
$$

If the water content in polythene is 2% and assuming direct proportionality, $\varepsilon_p = 2.25$, $\varepsilon_T = 3.75$ [8], $r_0 = 5$ micron, then $F_{wh} =$ $240 F_{\rm m}$.

This would indicate that the rate of growth of W.T. is a frequency dependent (F_w) . But it is sensitive to the amount of water content, and the original length of tree.

EXPERIMENTAL AND TESTING PROCEDURE

Samples: were casted from granules of polythene **(PE)** and **(XLPE)** at a temperature of 128°C in a disc form having a thickness of 10 mm. Seven holes were made in the sample by a needle of 5 μ m radius to a depth as shown in Figure 2a.

FIGURE 2a Specimen

Solutions: Distilled water of resistivity $1500 \Omega - m$, tap water Solutions: Distilled water of resistivity $1500 \Omega - m$ and sodium chloride $4 \Omega - m$ were used.

Test Cell: The high voltage electrode made of copper wire spring. The specimen was placed in a constant temperature bath at 25° C, as shown in Figure 2b. Solutions were poured with care not to produce bubbles.

A-C voltage was applied to the h.v. electrode starting from 1 kV and raised in steps of 0.5 kV/minute till the inception voltage was reached. The frequency of the voltage was variated as 50, 300, 1000, 3000, 8000 and **10,000Hz.** Tests were repeated with d-c voltages under same conditions.

TEST CELL **FIGURE 2b Test cell.**

Specimens were cut into wafers and then dyed with methylene blue dye to be examined under microscope. The wafers were removed from dye after 2 to 3 minutes, and placed into hot mild soapy water for one hour. Then cleaned with alcohol and dried gently.

RESULTS AND DISCUSSIONS

Inception Voltage: The inception stress, as calculated **[9],** showed a frequency dependence as shown in Figure 3.

As the frequency increased the inception stress decreases. The inception of trees sometimes show a time dependence after voltage

FIGURE *3* **Frequency dependence of inception voltage.**

application as shown in Figure **4,** which indicates a decrease in inception time as the applied voltage and its frequency was raised.

Water Tree Growth. Figure *5* shows that W.T., for a voltage applied for one hour, rate of growth increases as the voltage and frequency were raised. W.T. rate of growth increases with decreasing the resistivity of water solution Figure 6. W.T. disappeared when specimens were heated and reappeared when reimmersed in solution. The original tree length does affect the rate of growth. As the time of voltage application (under certain frequency, voltage and temperature) increases the rate of growth highly increases. But W.T. grows rapidly at the beginning and then continues at a slower rate.

W.T. Under Direct Voltages: When positive or negative d-c of the range 20 to 30 **kV** were applied, no W.T. was observed. This would show that W.T. is an a-c phenomena.

Mechanism of *Water Treeing:* Maxwell forces, due to normal field component, works as a compression to the polymer at the high field

APPLIED VOLTAGE, KV

FIGURE 4 Relation between induction time and applied voltage.

FIGURE 5 Relation between applied voltage and growth rate.

region near the needle tip [9]. Then an induced stress perpendicular to the field direction may appear in polymer. When this stress exceeds a critical value, crazing action may take place from the micro-voids. When a gas discharges in a void-crack it forms an electric field more than the electric strength of the polymer at the apex of the void, and microscopic tree channel may appear due to the partial breakdown of polymer.

Dielectric loss and Joule heating make water to evaporate that increase in pressure and temperature which cause damage. The rate of rise in temperature due to dielectric losses in water is **1"C/s** at a field of 10.

 MV/m , 50 Hz [10]. The temperature rise may lead to vaporization or thermal degradation of water and PE when voltage is applied. When a-c field is applied water as (H_2O) _n may undergo lattice vibrations that gets it decomposed into molecular groups (clusters). These clusters may penetrate into microvoids extending across molecules of PE by Maxwell force.

FIGURE 6 Relation between growth rate and time of voltage application.

CONCLUSIONS

It is concluded that W.T. inception is frequency dependent. The growth of trees depends on the applied voltage, frequency and the electrical resistivity of solution. W.T. initiates and grows by penetration of clusters into the microvoids due to Maxwell stress and the dielectric loss and Joule heating make water expand and evaporate so that the increase in pressure and temperature may cause damage. Also the ionization discharges in clusters may cause more damage.

The growth rate frequency dependence is not solely explained by the frequency factor Fw obtained from theory.

The experimental results are consistent with theory and it can explain W.T. characteristics.

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